Justification of dead zone presence in catalyst pellets.

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Abstract – Heterogeneous catalytic processes and biocatalitic processes are the most important types of the processes where existence of zones without reactants were reported. The aim of the work is justification of presence of dead zone in the catalyst pellet by experimental verification of a model solution. Good consistency of theretical and experimental results justify that dead zone is present inside the catalyst pellet.

Keywords – heterogeneous catalysis, dead zone, dead core, effectiveness factor, diffusional resistances

Introduction

Heterogeneous catalytic processes and biocatalitic processes are the most important types of the processes where existence of zones without reactants were reported. And we don't think about physical defects of catalysts resulted mainly from imperfections of manufacturing or activation processes regions of catalysts or biofilms without reactants that arise spontaneously as a result of fast reaction run, despite the fact that in this area catalyst or bio-catalyst (enzyme) could be active. The inactive zone lessens reactor or bioreactor productivity and influences on process economy –it can reduce or even destroy in large scale processes effects obtained in laboratory. For heterogeneous catalysis the zone without reactants was called "dead zone" and it was predicted by Aris[1]. The analytic solution of non-linear problem without external mass transfer limitations and without the dead zone was presented by Mehta and Aris [2] while for the presence of dead zone by York et al. [3]. Szukiewicz [4] extends applicability region of these solutions on the case of important external mass transfer resistances. The aim of the work is justification of presence of dead zone in the catalyst pellet by experimental verification of a model solution.

Results and Discussion

Catalytic micro-reactor (the Microactivity Effi reactor, PID Eng&Tech, Spain) of diameter 9.1 mm equipped with hydrogen generator, was used for investigations. In the reactor was carried out hydrogenation of propylene. As a hydrogenation catalyst the KUB-3 catalyst (the main components of the catalyst are Ni, NiO, and Al₂O₃.) manufactured by INS, Puławy, Poland was chosen. Catalyst form: plate with diameter 4-6 mm and thicknes 0.4 mm. Experiments were carried out at temperature range 100-150°C under pressure 1.2×10⁵Pa.

On the basis of experiments carried out the following kinetic equation was developed:

$$r_p = 44400 p_p^{0.5} e^{\frac{-26500}{RT}} \quad [\text{mol/}(m^3 \text{ s})](1)$$

The kinetic equation indicates that inside the catalyst pellet a dead zone can be formed. Consequently, a mathematical model of the process includes typical mass balance equation with boundary conditions characteristic for dead zone problem [1]. The analytic solution for the problem under consideration is given by:

$$c = \left(\frac{1-n}{2} \sqrt{\frac{2\Phi^2}{1+n}}\right)^{2/(1-n)} (x - x_{dz})^{2/(1-n)}$$
 (2)

where Φ is Thiele modulus, n is an exponent in the kinetic equation. x_{dz} (coordinate that determines dead zone location) and c_s (surface concentration) can be determined from:

$$1 - x_{dz} = \frac{2}{1 - n} \sqrt{\frac{1 + n}{2 + 2}} c_s^{(1 - n)/2} \text{ and } \sqrt{\frac{2 + 2}{1 + n}} c_s^{(1 + n)/2} = Bi_m (1 - c_s)$$
 (3)

Effectiveness factor is given by

$$\eta = \sqrt{\frac{2c_s^{1+n}}{(1+n)\Phi^2}} \quad (4)$$

Effectiveness factor values calculated theoretically and determined from experiment were compared. Results are presented in Table 1. The calculated and determined experimentally values of effectivess factor have close values. The error does not exceed 10% (with one exception – E9) so consistency of results can be treated as good. Determined size of dead zone was about 75%, so a greater part of catalyst pellet remains inactive.

Table 1 Experimental and theore	rtical values of effectiveness fact	tor
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Exp.	Molar	Temp.	$D_{ef} \cdot 10^7$	k_{g}	η_{exp}	$\eta_{ m calc}$
number	ratio	[°C]	$[m^2/s]$			
E1	0.10	101.4	2.95	0.178	0.0709	0.0780
E2	0.14	111.2	3.58	0.210	0.0669	0.0828
E3	0.12	111.3	3.58	0.196	0.0759	0.0794
E4	0.14	120.3	3.81	0.214	0.0856	0.0765
E5	0.16	120.0	3.81	0.228	0.0840	0.0796
E6	0.20	130.0	3.73	0.424	0.0840	0.0752
E7	0.14	142.0	3.79	0.275	0.0919	0.0925
E8	0.20	141.5	3.79	0.327	0.0986	0.1024
E9	0.20	151.0	3.94	0.439	0.0758	0.0618

Conclusion

Good consistency of theretical and experimental results justify that dead zone is present inside the catalyst pellet since presented in References regular and dead zone model are complementary.

Acknowledgments

The financial support of the National Science Centre, Poland (Project 2015/17/B/ST8/03369) is gratefully acknowledged.

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